

QUIZ 12

NAME: _____

- 1) (10 PTS.) Find the coordinates of the x -intercept and of the y -intercept of the line given by $3x + 4y = 18$.

y -intercept:

$$x=0 \Rightarrow 3 \cdot 0 + 4y = 18 \Rightarrow y = \frac{18}{4} = \frac{9}{2}$$

x -intercept

$$y=0 \Rightarrow 3x + 4 \cdot 0 = 18 \Rightarrow x = 6$$

Answer: x intercept = (6, 0) y intercept = (0, $\frac{9}{2}$)

- 2) (20 PTS.) Find the equation of the line that passes thru the points $(3, -2)$ and $(2, 10)$. Express your answer in the form $y = mx + b$ by filling in the blanks below for the values of m and b .

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{10 - (-2)}{2 - 3} = \frac{12}{-1} = -12$$

$$\Rightarrow y = -12x + b$$

SUBSTITUTE $x=3, y=-2$

$$-2 = -12 \cdot 3 + b$$

$$-2 = -36 + b$$

$$34 = b$$

Check:

$$-2 = -12 \cdot 3 + 34 \quad @ (3, -2)$$

$$10 = -12 \cdot 2 + 34 \quad @ (2, 10)$$

Answer: Fill in the blanks: $y =$ -12 $x +$ 34

3) (20 PTS.) Find the point of intersection of the two lines given by $2x + 10y = 4$ and $5x + 2y = -1$.

$$\begin{array}{r} \begin{array}{l} 2x + 10y = 4 \\ 5x + 2y = -1 \end{array} \\ \begin{array}{l} \times 5 \\ \times 2 \end{array} \end{array} \begin{array}{r} 10x + 50y = 20 \\ 10x + 4y = -2 \end{array} \begin{array}{r} \\ - \end{array}$$

$$0x + 46y = 22$$

$$y = \frac{22}{46} = \frac{11}{23}$$

SUBSTITUTE THIS INTO $2x + 10y = 4$

$$2x + 10 \cdot \frac{11}{23} = 4$$

$$\begin{aligned} x &= \frac{4 - \frac{110}{23}}{2} = 2 - \frac{55}{23} = \frac{46}{23} - \frac{55}{23} \\ &= \frac{9}{23} \end{aligned}$$

Answer: $\left(\frac{9}{23}, \frac{11}{23} \right)$