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LINEAR PROGRAMMING

EXAMPLE 7.3



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value of his activites

An account executive divides his time between

YOU GET TO CHOOSE HOW MANY HOURS ARE DEVOTED TO EACH **ACTIVITY**

What are the activities?????







Lecture 27

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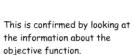
It looks like the activities are:

1) sales 2)support



3

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Question: Are "paperwork and reading" sales and support activities?

Answer: No, they are support activities only, as can be seen by reading the next two sentences.

What are the activities?????

It looks like the activities are:

1) sales 2)support







5



value of his activites

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y ≥ 5 +







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y ≥ 5 + .1x







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 $x + y \le 50$



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@ ERASE

What does this mean?

 $x + y \le 50$





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sales all work x ≥ .5(x + y)

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15

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sales all work x ≥ .5(x + y)

"but there is . . ." ??????????????

 $x + y \le 50$

value of activities =

15x + 10y

This must be the objective function. It is what you are trying to maximize.









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Maximize





Lecture 27

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Maximize

15x + 10y

Subject to:

y ≥ 5 + .1x

 $x \ge .5(x + y)$

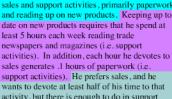
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x = # hours devoted to sales y = # hours devoted to support

15x + 10y

Maximize

15x + 10y

Subject to:

 $y \ge 5 + .1x$ y - .1x ≥ 5

 $x \ge .5(x + y)$.5x - .5y ≥ 0

x + y ≤ 50 $x + y \le 50$



@ ERASE





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Maximize

15x + 10y

Subject to:

 $y \ge 5 + .1x$ $y - .1x \ge 5$

x ≥ .5(x + y) x - y ≥ 0

x + y ≤ 50 $x + y \le 50$











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Maximize

15x + 10y

Subject to:

y - .1x ≥ 5

 $x - y \ge 0$

 $x + y \le 50$

x > 0y ≥ 0





x = # hours devoted to sales y = # hours devoted to support

Maximize 15x + 10y Subject to:

 $y - .1x \ge 5$

x - y ≥ 0

 $x + y \le 50$

x ≥ 0

y ≥ 0

@ ERASE







x = # hours devoted to sales y = # hours devoted to support

devoted to each activity that maximizes the

Maximize

value of his activites

15x + 10y Subject to:

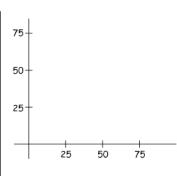
y - .1x ≥ 5

x - y ≥ 0

 $x + y \le 50$

x ≥ 0

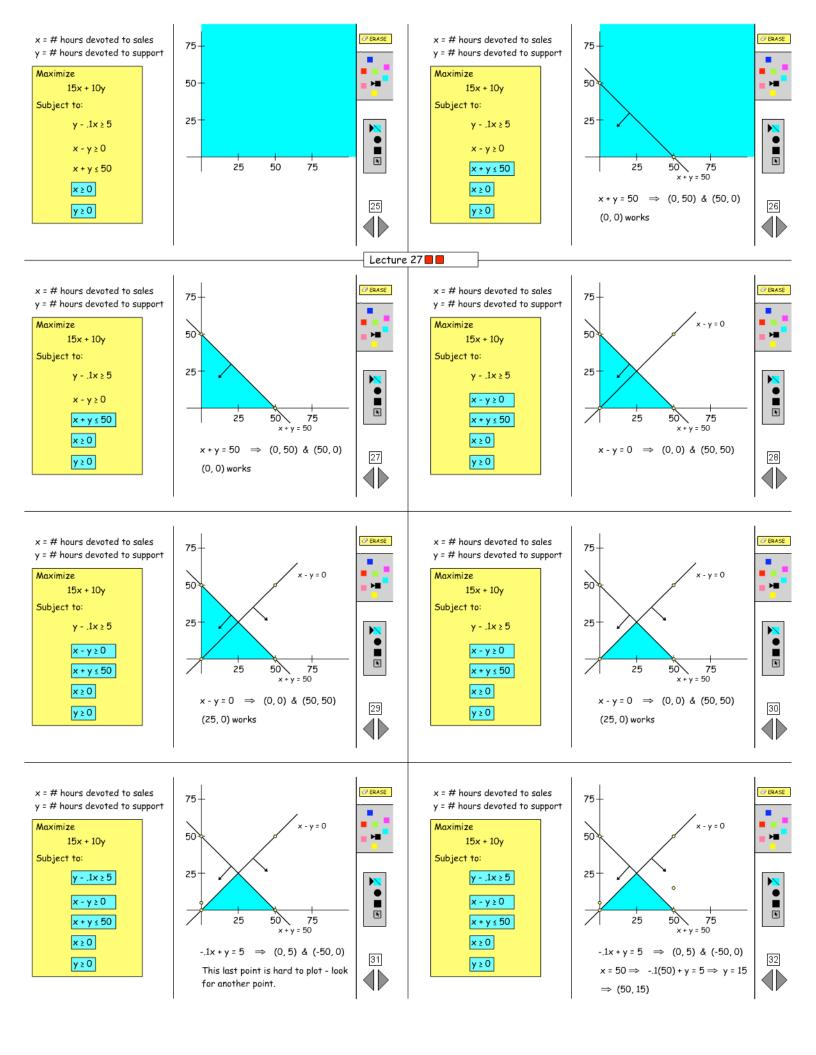
y ≥ 0

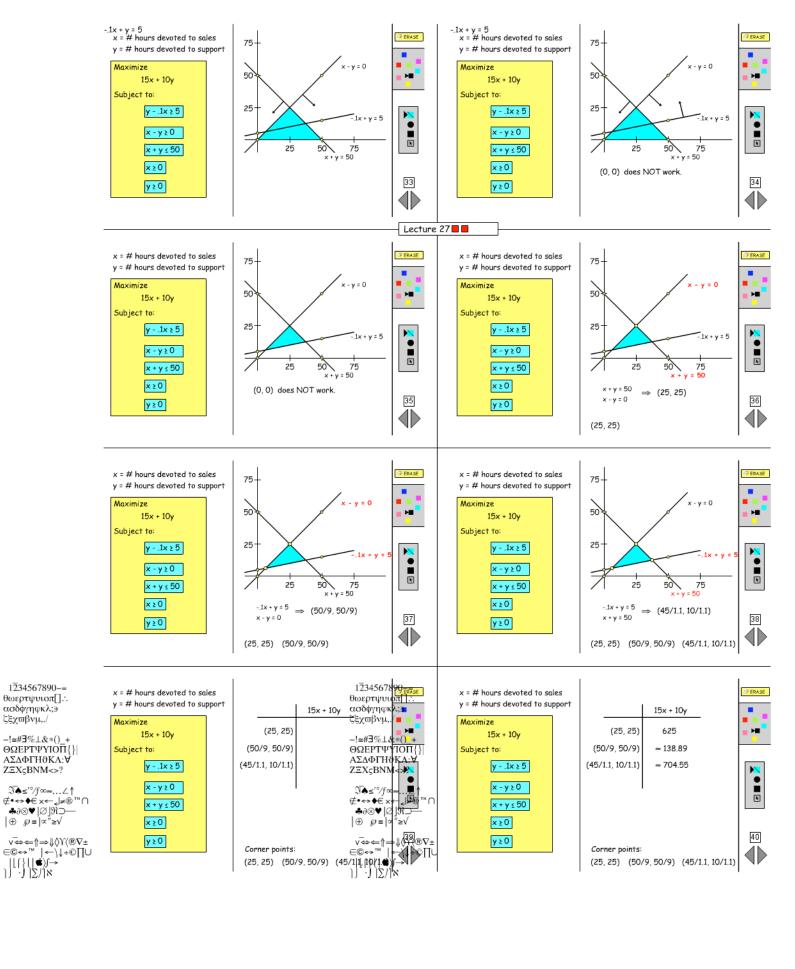












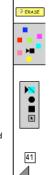
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x = # hours devoted to sales y = # hours devoted to support

Maximize 15x + 10y Subject to: y - .1x ≥ 5 x - y≥0 x + y ≤ 50 x ≥ 0

	15x + 10y
(25, 25)	625
(50/9, 50/9)	≈ 138.89
(45/1.1, 10/1.1)	≈ 704.55

So the maximum value of the work done is \$704.55, and this is achieved by working $45/1.1 \approx 40.9$ hours on









	y≥O	sales and 10/1.1 ≈ 9.1 hours on support, for a total of 50 hours per week.	41		42
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